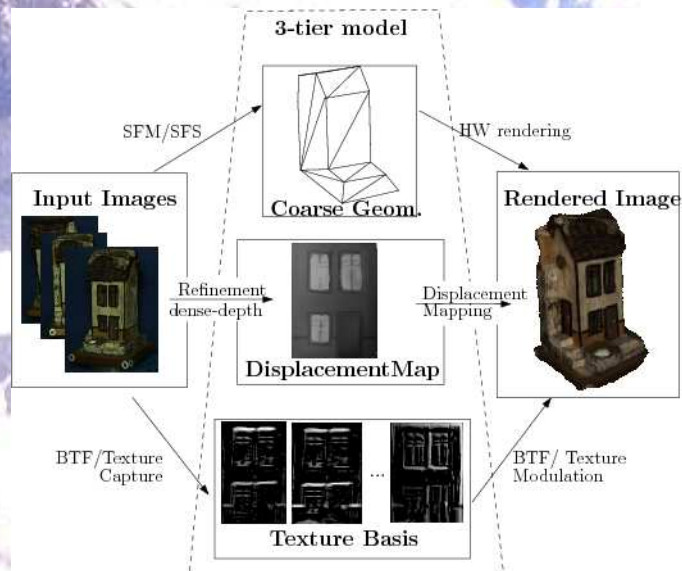
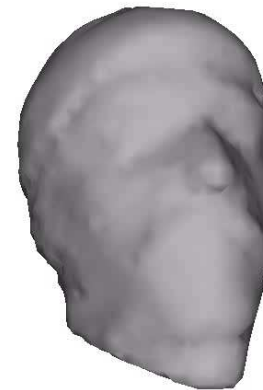


Computing models of 3D geometry and appearance for photo-realistic rendering

Martin Jagersand,



```
sigma = 0.024592  
sigma = 0.025011  
remesh 10  
remesh 10  
remesh 10  
remesh 10  
remesh 10  
writing 1
```



video

Low budget 3D from video example

Capture objects

- Inexpensive
- Quick and convenient for the user
- Integrates with existing SW e.g. Blender, Maya

Low budget 3D from video

- Inexpensive



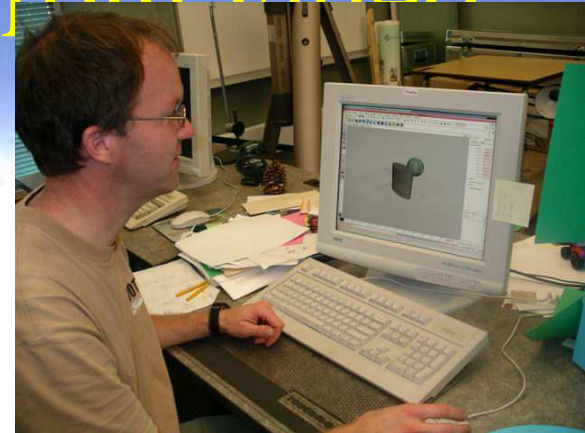
\$100: Webcams, Digital Cams



\$100,000 Laser scanners etc.

Low budget 3D from video

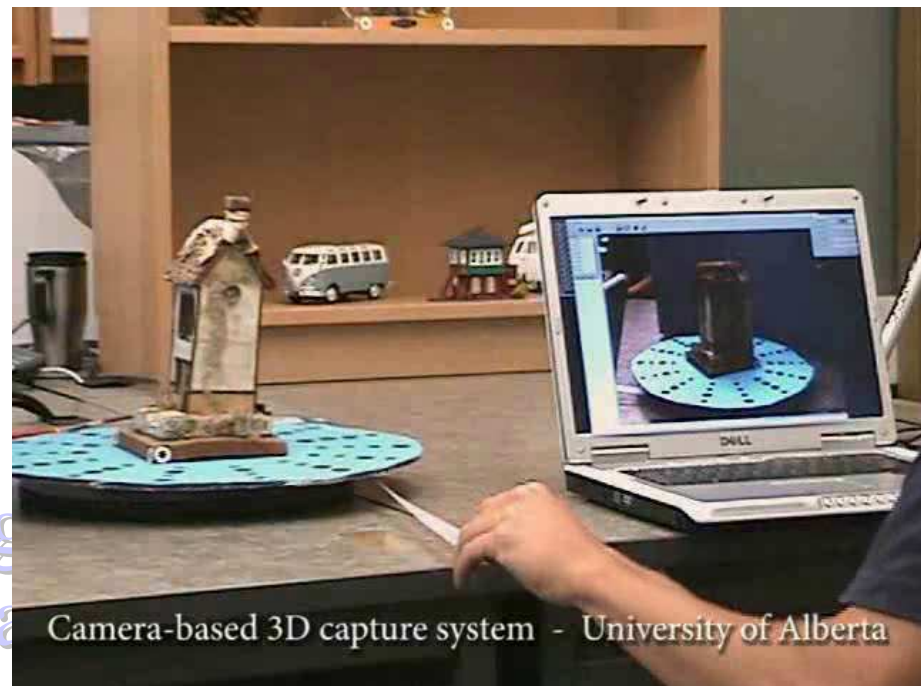
- Inexpensive



Modeling geom primitives into scenes: >>Hours

- Quick and convenient for the user

- Integrates with existing SW e.g. Blender, Maya



Capturing 3D from 2D video: minutes

Low budget 3D from video

- Inexpensive
- Quick and convenient for the user
- Integrates with existing SW e.g. Blender, Maya



Application Case Study Modeling Inuit Artifacts

Martin Jagersand
U of Alberta

- New acquisition at the UofA: A group of 8 sculptures depicting Inuit seal hunt
- Acquired from sculptor by Hudson Bay Company

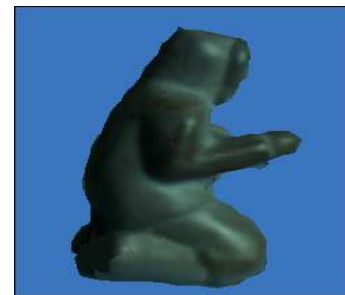


Application Case Study Modeling Inuit Artifacts

Martin Jagersand
U of Alberta

Results:

1. A collection of 3D models of each component

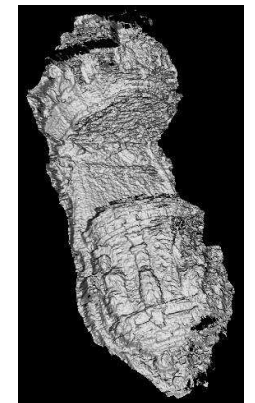
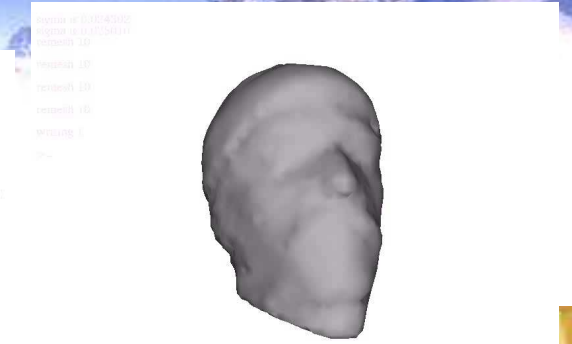
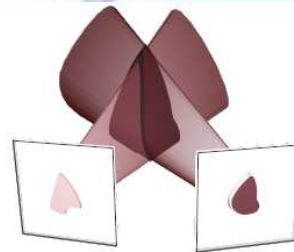


2. Assembly of the individual models into animations and Internet web study material.



Preliminaries: Capturing Macro geometry:

- **Shape From Silhouette**
 - Works for objects
 - Robust
 - Visual hull not true object surface
- **Structure From Motion**
 - Works for Scenes
 - Typically sparse
 - Sometimes fragile (no salient points in scene)
- **Space carving**
 - Use free space constraints
- **Global Dense Refinement**
 - Variational PDE
 - Use as second refinement step



Incremental Free-Space Carving

2D Example

Cameras

Freespace

Uncarved/
occupied

In 3D: Triang → Tetrahedra

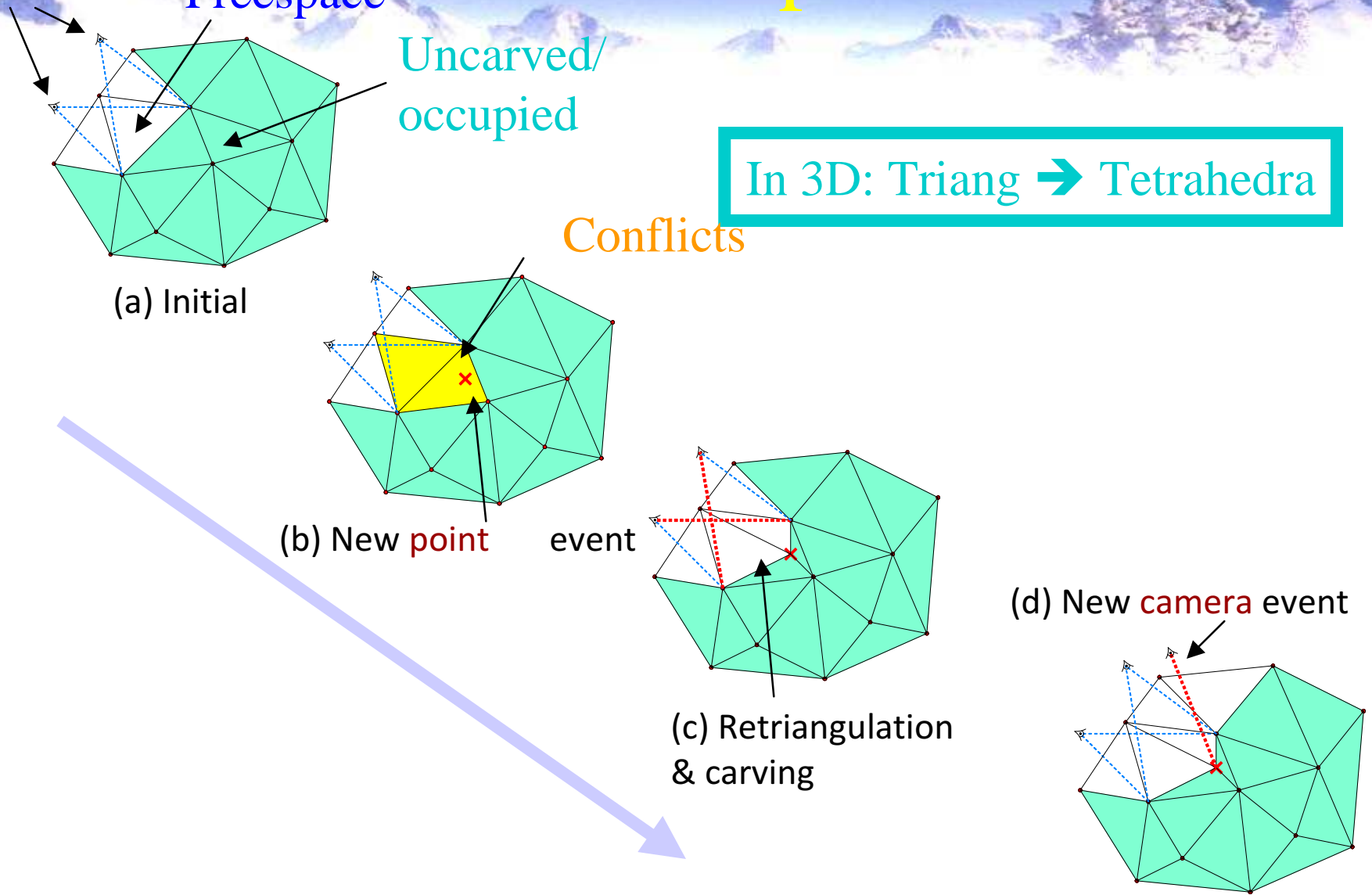
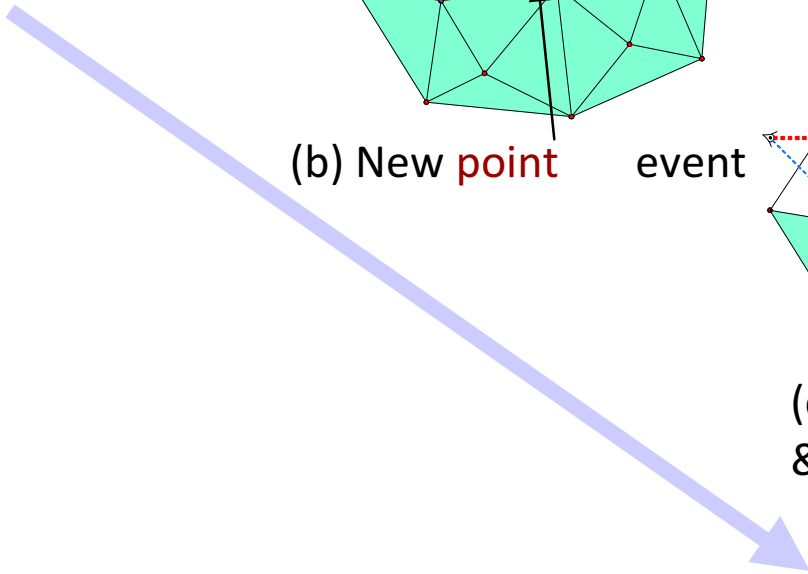
Conflicts

(a) Initial

(b) New **point** event

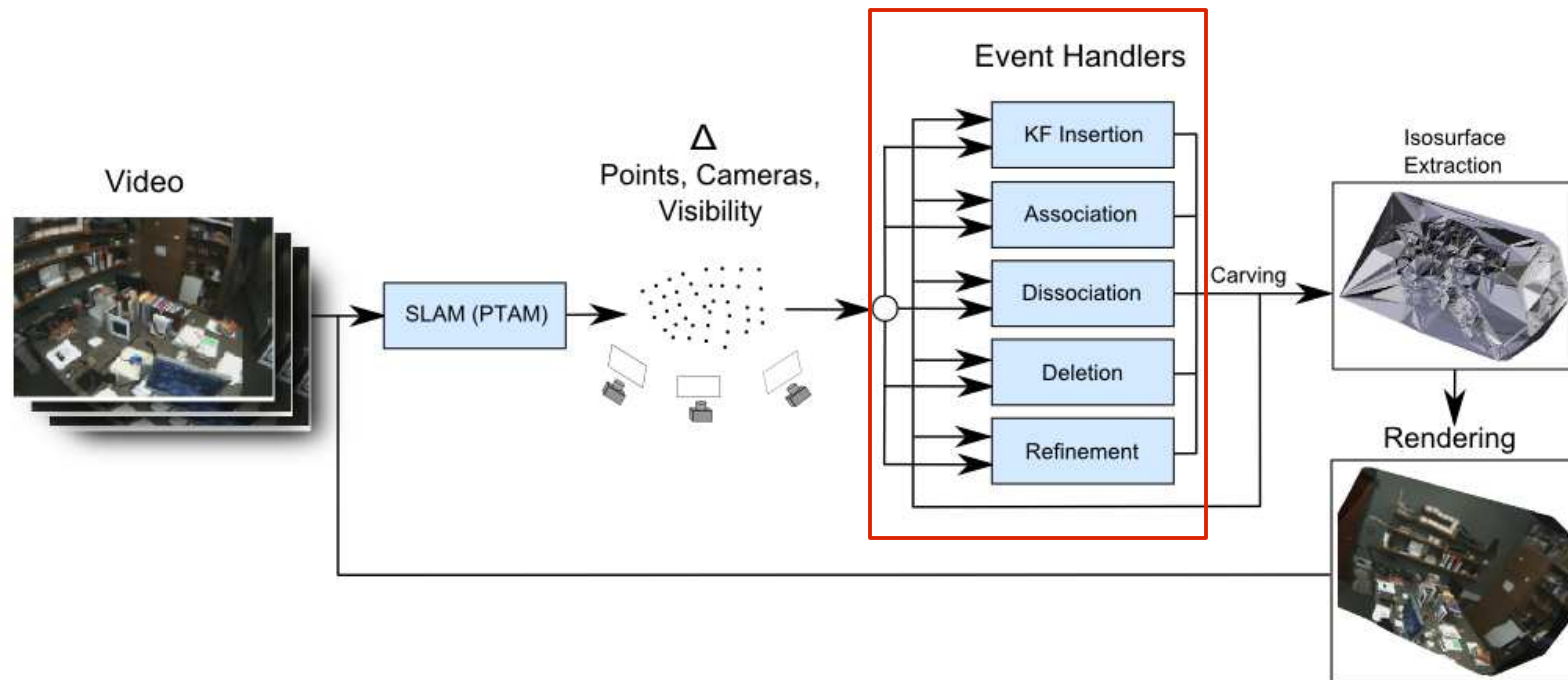
(c) Retriangulation
& carving

(d) New **camera** event

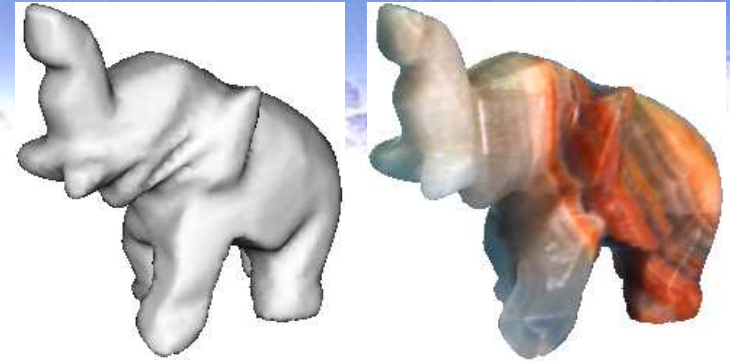


3D Modeling System

- Online, incremental handling of **new-information** events
 - Inputs continuously change online
 - Different types of changes trigger tailored processing

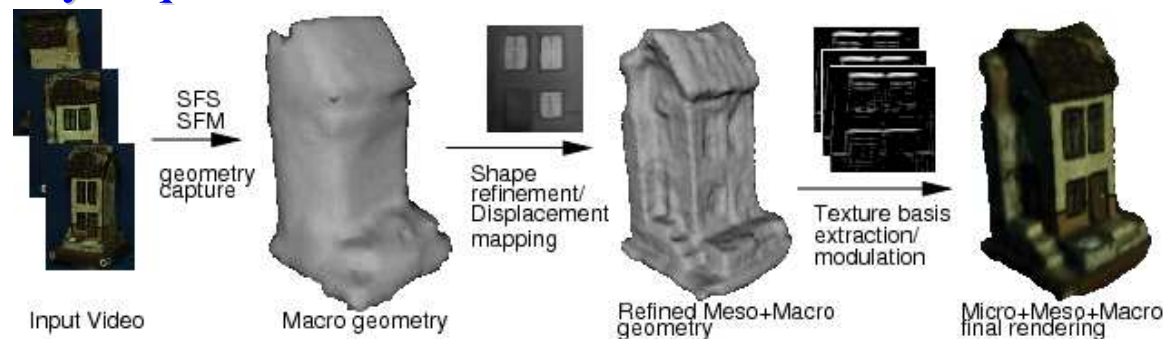


3-tier Macro, Meso, Micro model

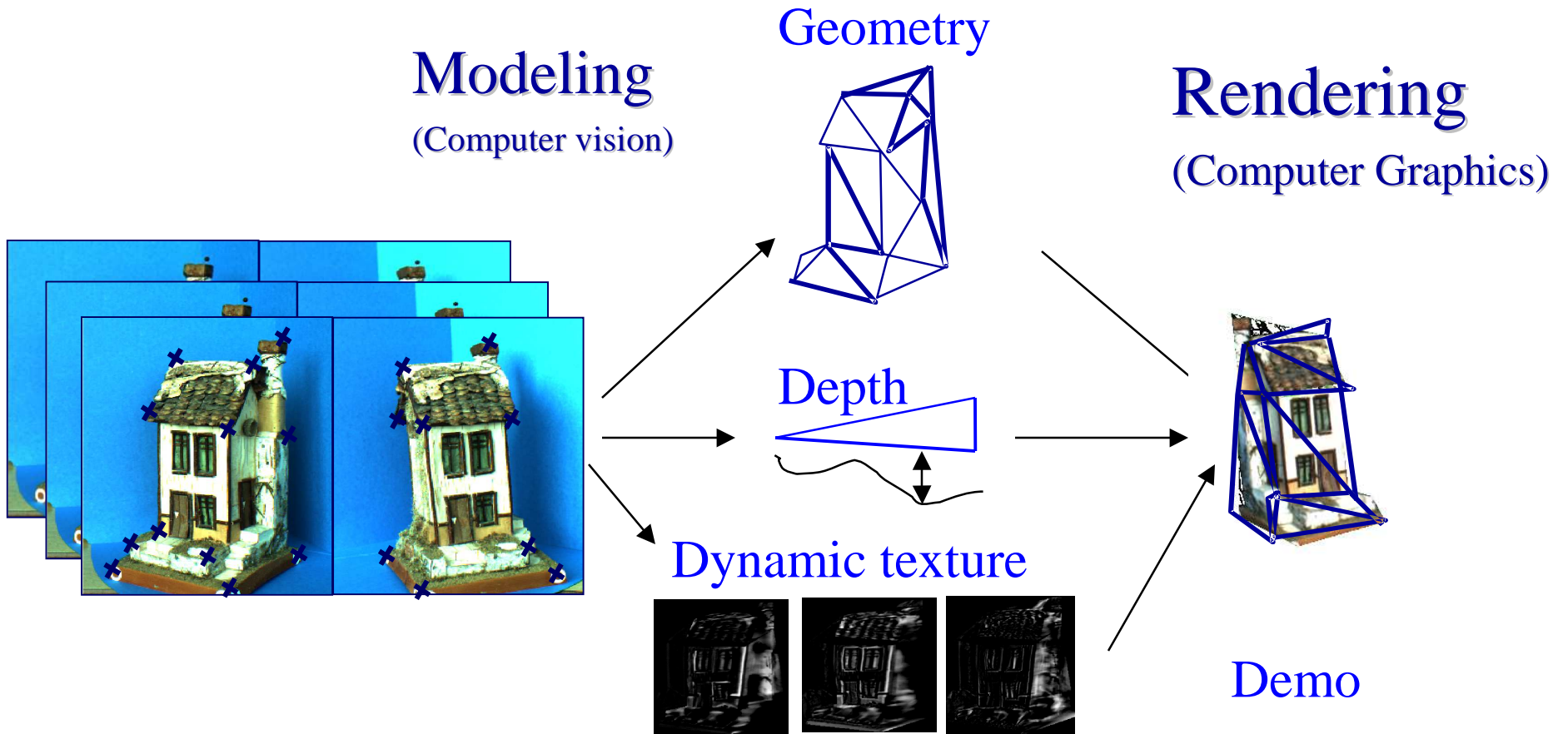


- **Multi-Tiered Models:**

- **Commonly:**
 - Two tiers: 3D Geometry and appearance (* texture mapping)
 - Used in graphics applications, recovered in Vision applications
- **Three-Tier**
 - Macro scale: describes scene geometry (triangulated mesh)
 - Meso scale: fine scale geometric detail (displacement map)
 - Micro: fine scale geometry and reflectance (Texture basis)
- **Captured by sequential refinement**

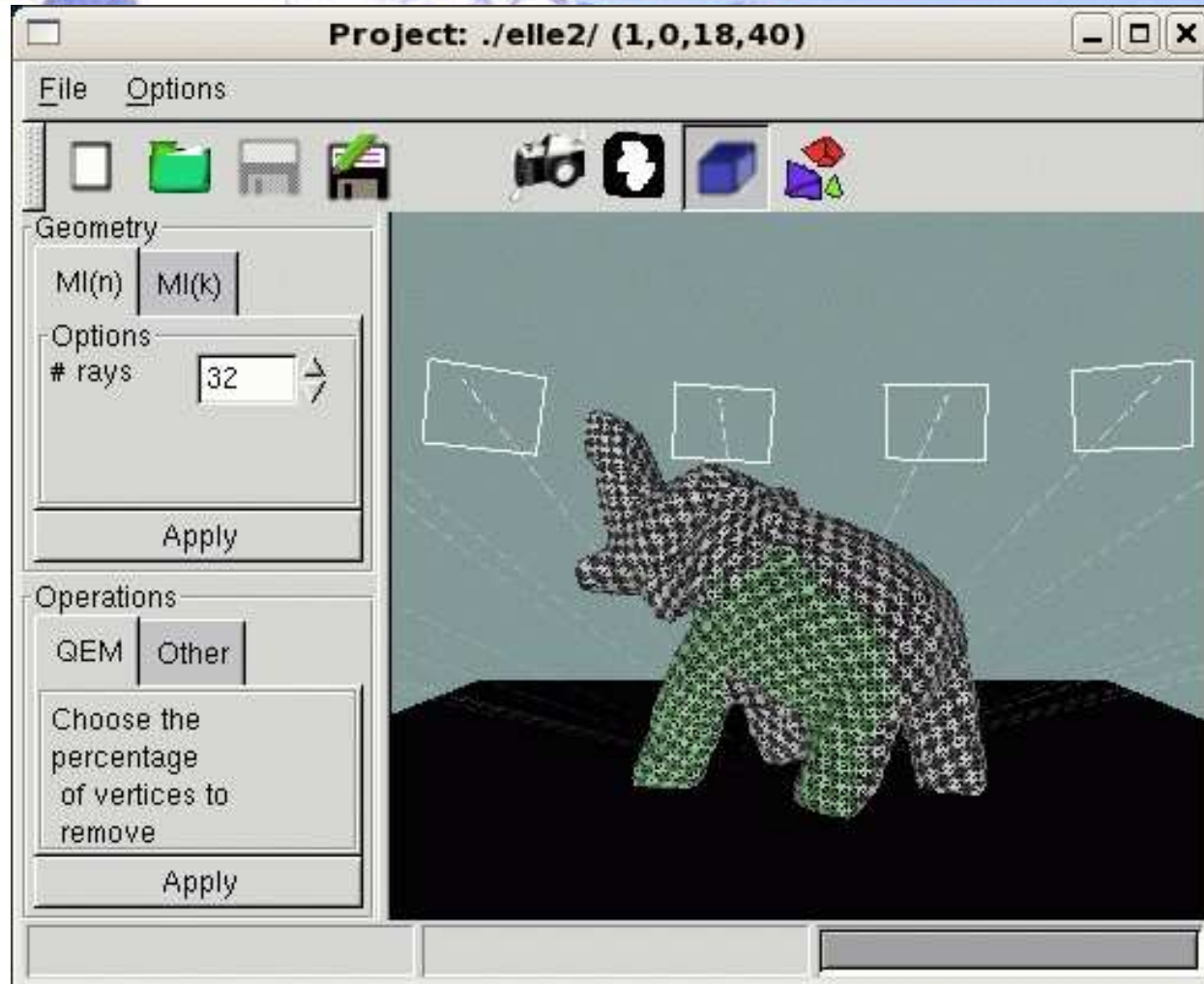


Geometry alone does not solve modeling! Need: Multi-Scale Model



Multi-Scale model: **Macro** geometry, **Meso** depth, **Micro** texture

Capgui Demo



Capgui demo

CAMERA-BASED 3D CAPTURE SYSTEM

Step 1 Calibration

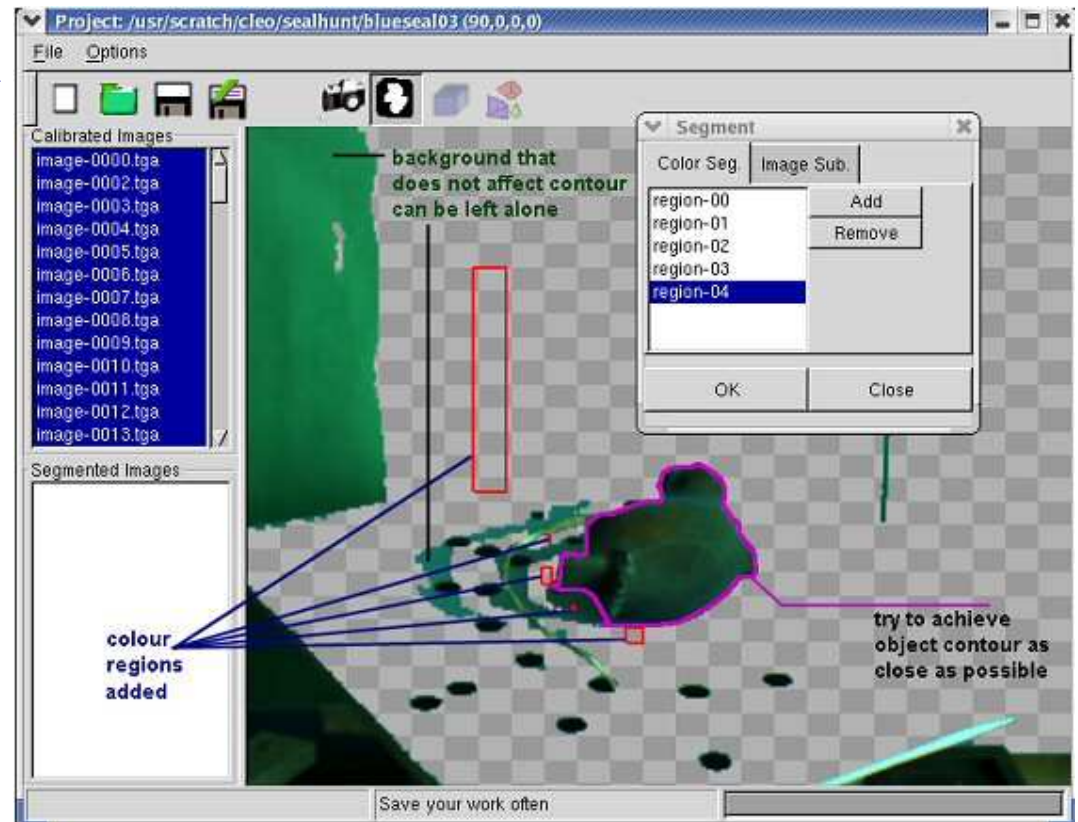
Compute camera – object pose

- Flat radial calib pattern
 - Rotating all-around capture
- Each row a unique code
- Crossratio projective invariant

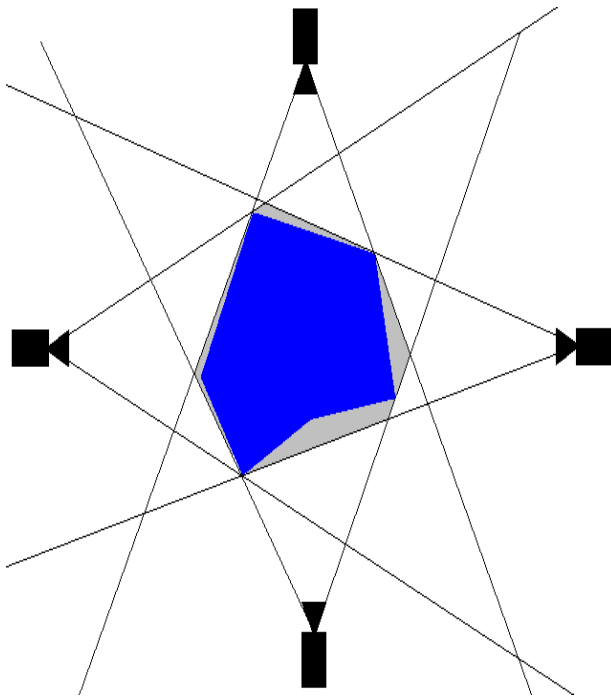
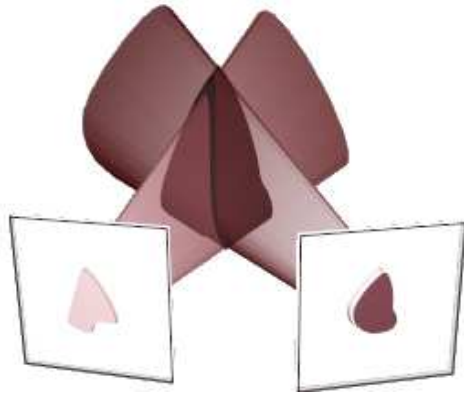


Step 2 Segmentation

- Background removal
- PCA model
 - see tracking lectures
- One or more pixel samples

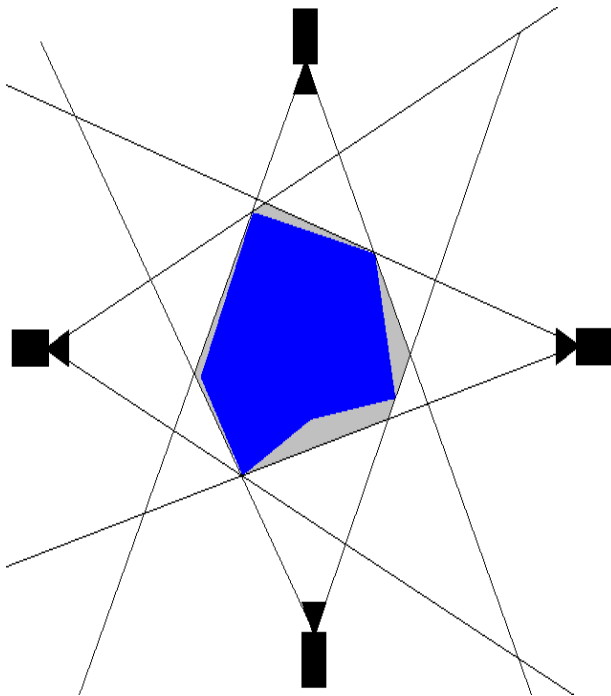
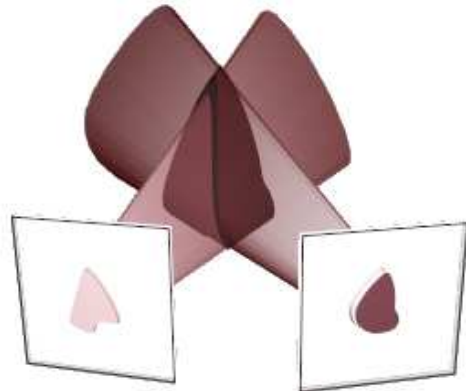


Step 3: Shape From Silhouette



- With multiple views of the same object, we can intersect the *generalized cones* generated by each image, to build a volume which is guaranteed to contain the object.
- The limiting smallest volume obtainable in this way is known as the *visual hull* of the object.
- Use 8 - 60 images

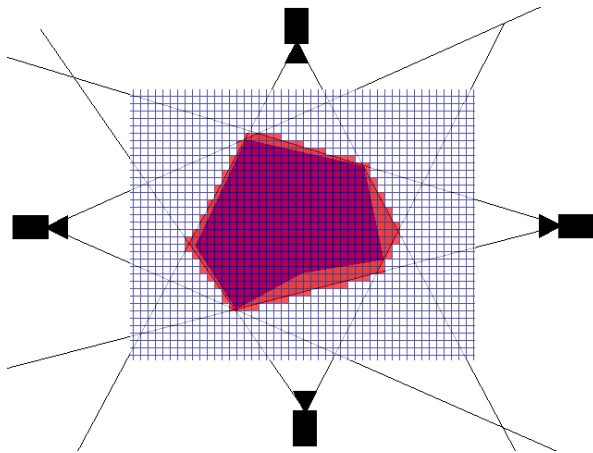
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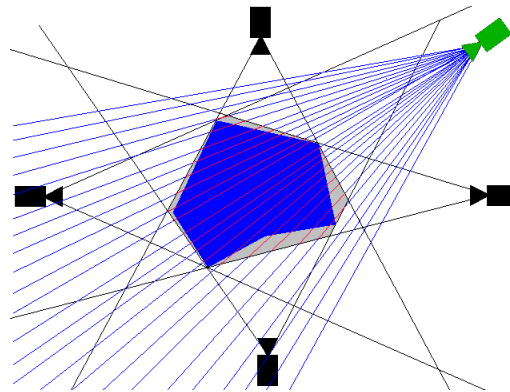
SFS Methods

Voxel-based



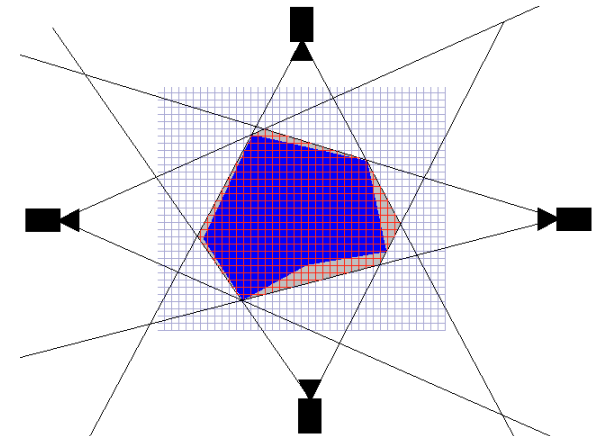
- Inaccurate
- + Triangulate w. marching cubes

Image ray based



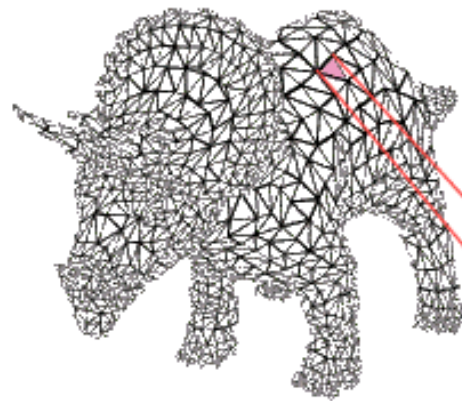
- + Accurate

Axis-aligned

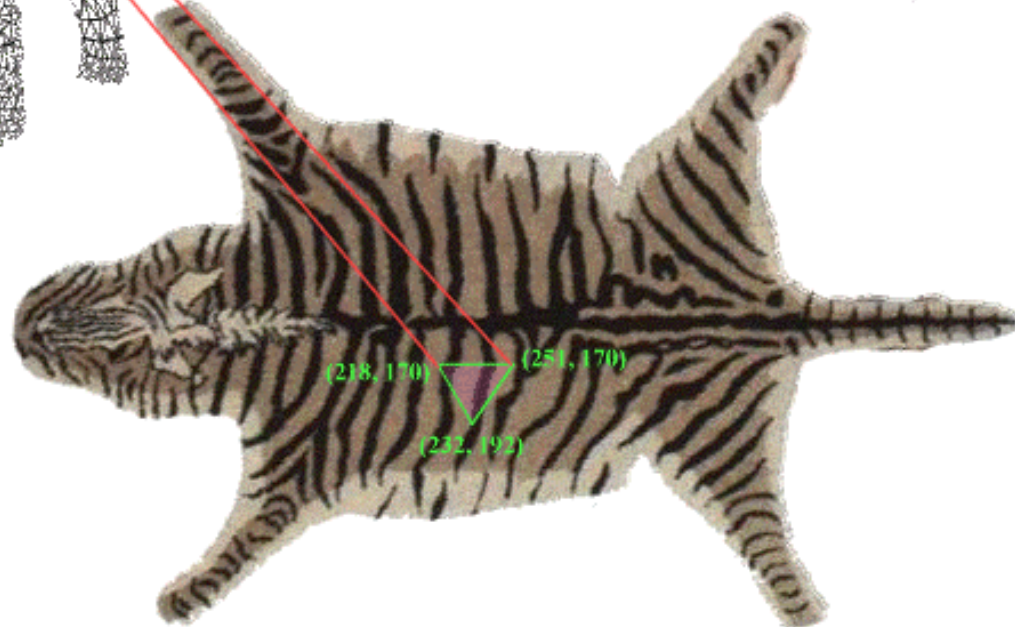


- Moderately accurate
- + Fast
- + Marching intersections

Step 4 Photo-textures and texture mapping



*For each triangle in the model
establish a corresponding region
in the phototexture*



*During rasterization interpolate the
coordinate indices into the texture map*

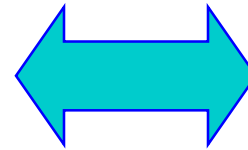
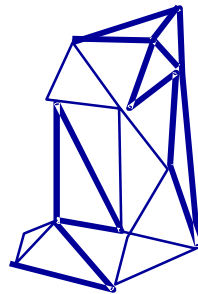
Simple models can be manually flattened

3D geometry and texture warp map between views and texture images

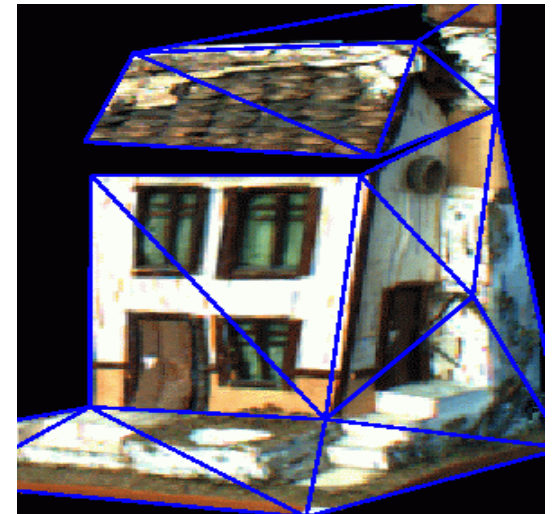
View



Re-projected
geometry



Texture



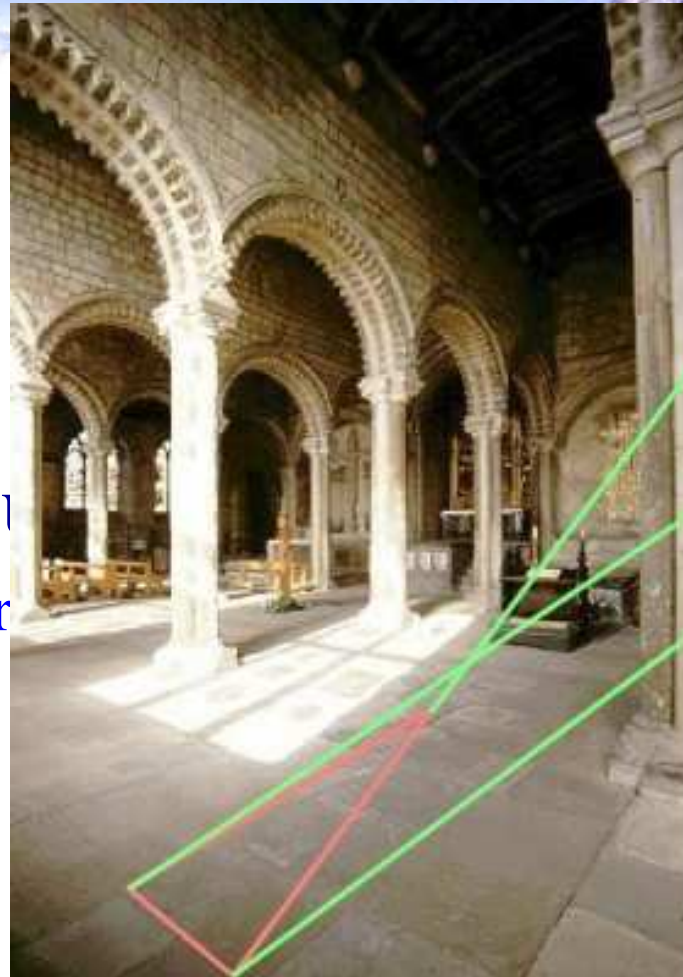
Texture
coordinate
warp

1₁

t

Texture Mapping Difficulties

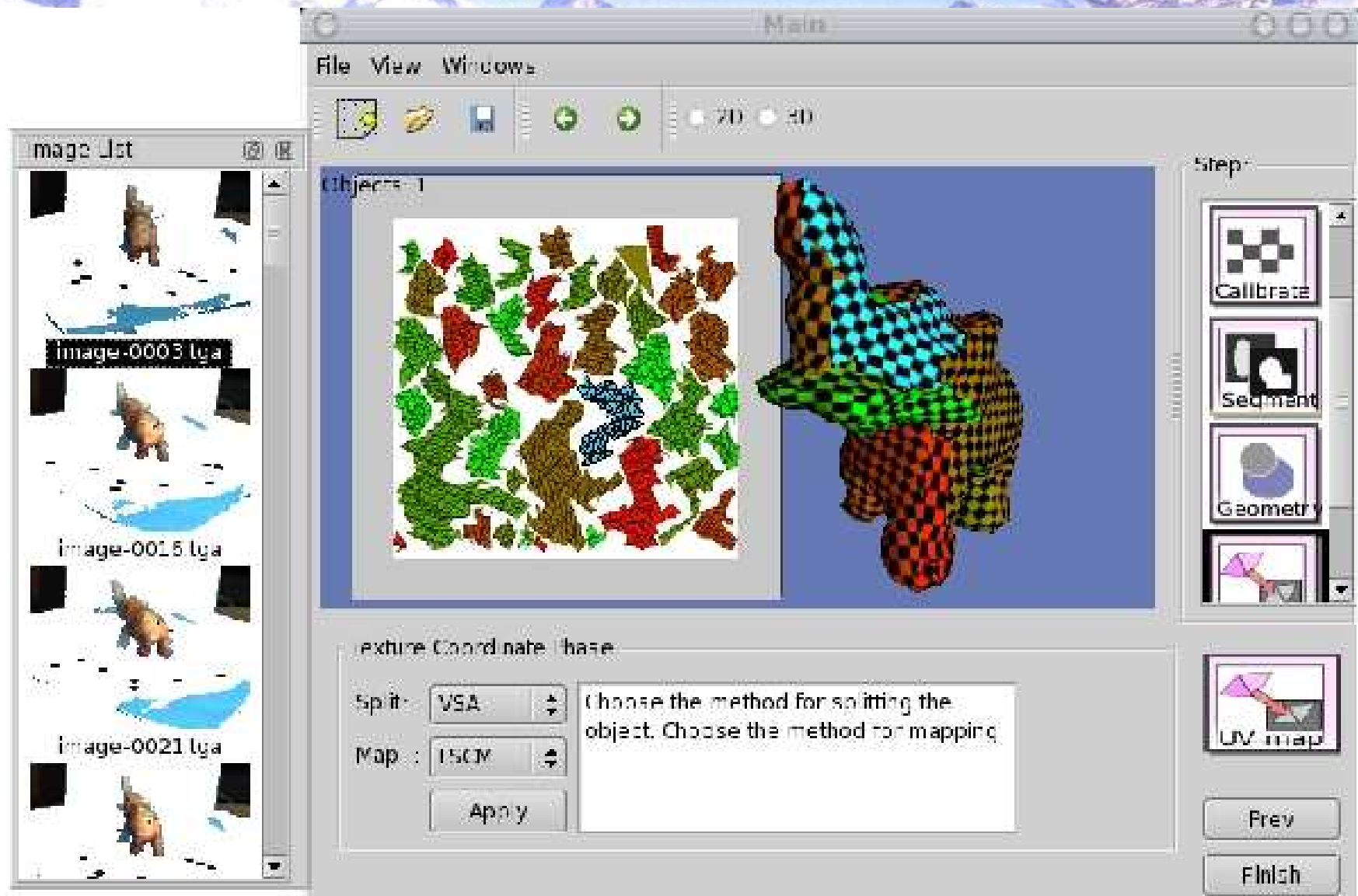
- Tedious to specify texture coordinates for every triangle
- Acquiring textures is slow
 - Texture image can't have perspective
 - Seamless tiling
 - Non-repeating textures



*Can't
do this!*

*You can get around
this problem for
planar surfaces if
you specify 4 points...*

Complex, detailed models: Automatic texture split and flatten



Common Texture Coordinate Mappings

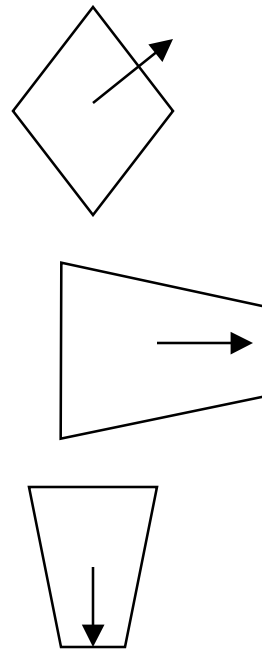
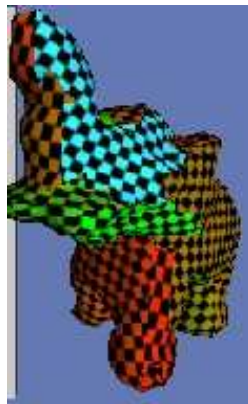
- Orthogonal
- Cylindrical
- Spherical
- Perspective Projection
- Texture Chart



Advanced texture splitting and mapping

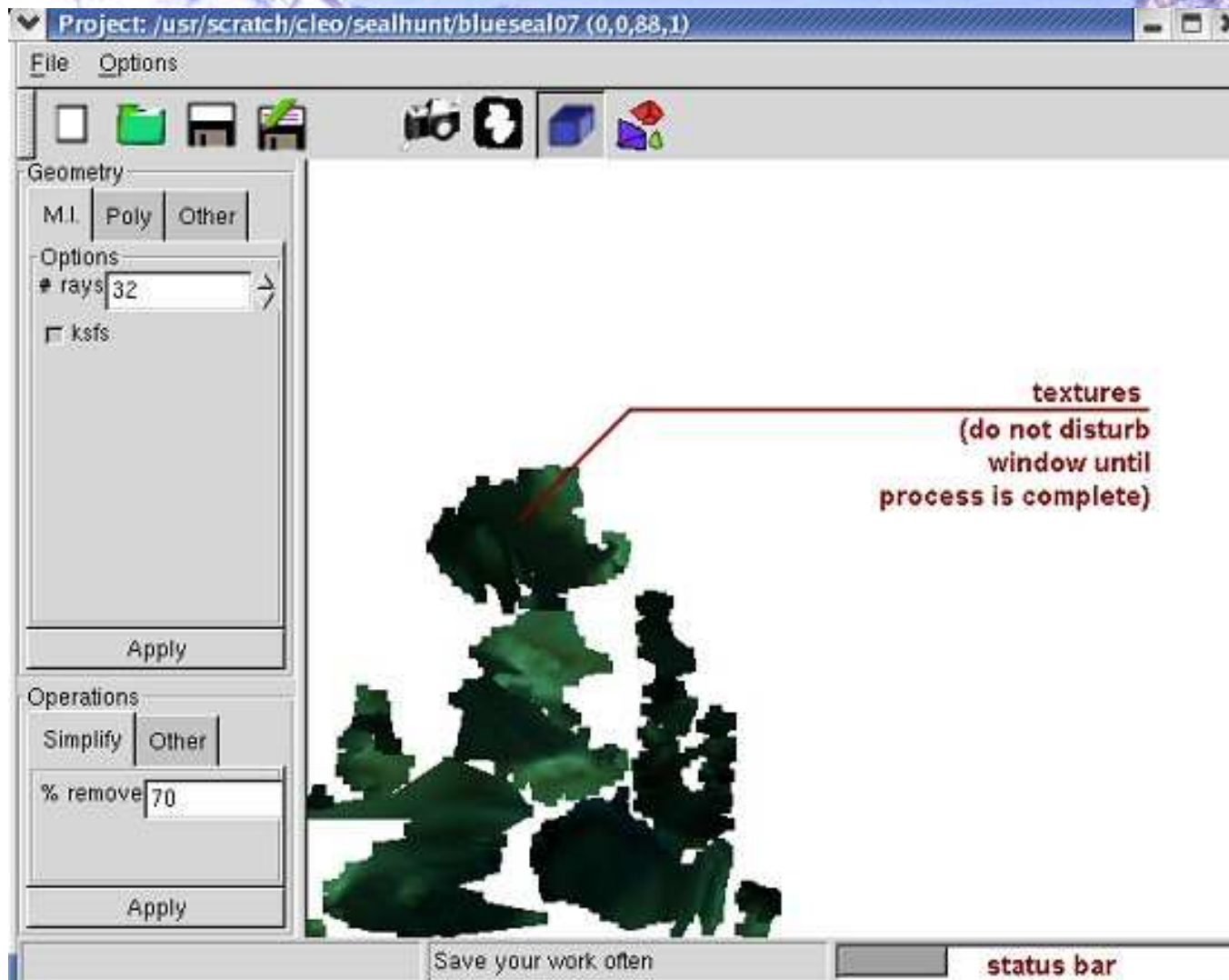
Martin Jagersand
U of Alberta

- Floating Planes (Mathieu Desbrun, INRIA, CalTech)



- LCSM: Least Squares Conformal Mapping

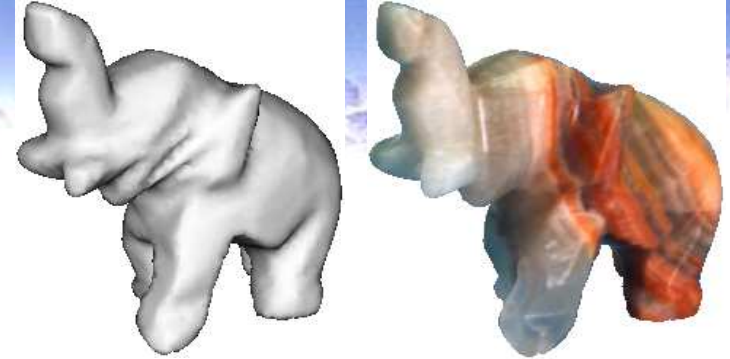
Step 6 Texture basis computation



Dyntext theory

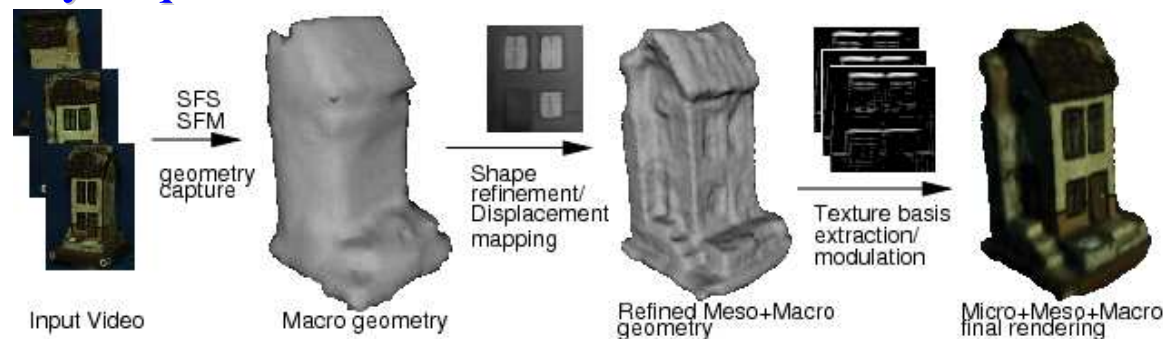
- Dyntext slides start here

3-tier Macro, Meso, Micro model

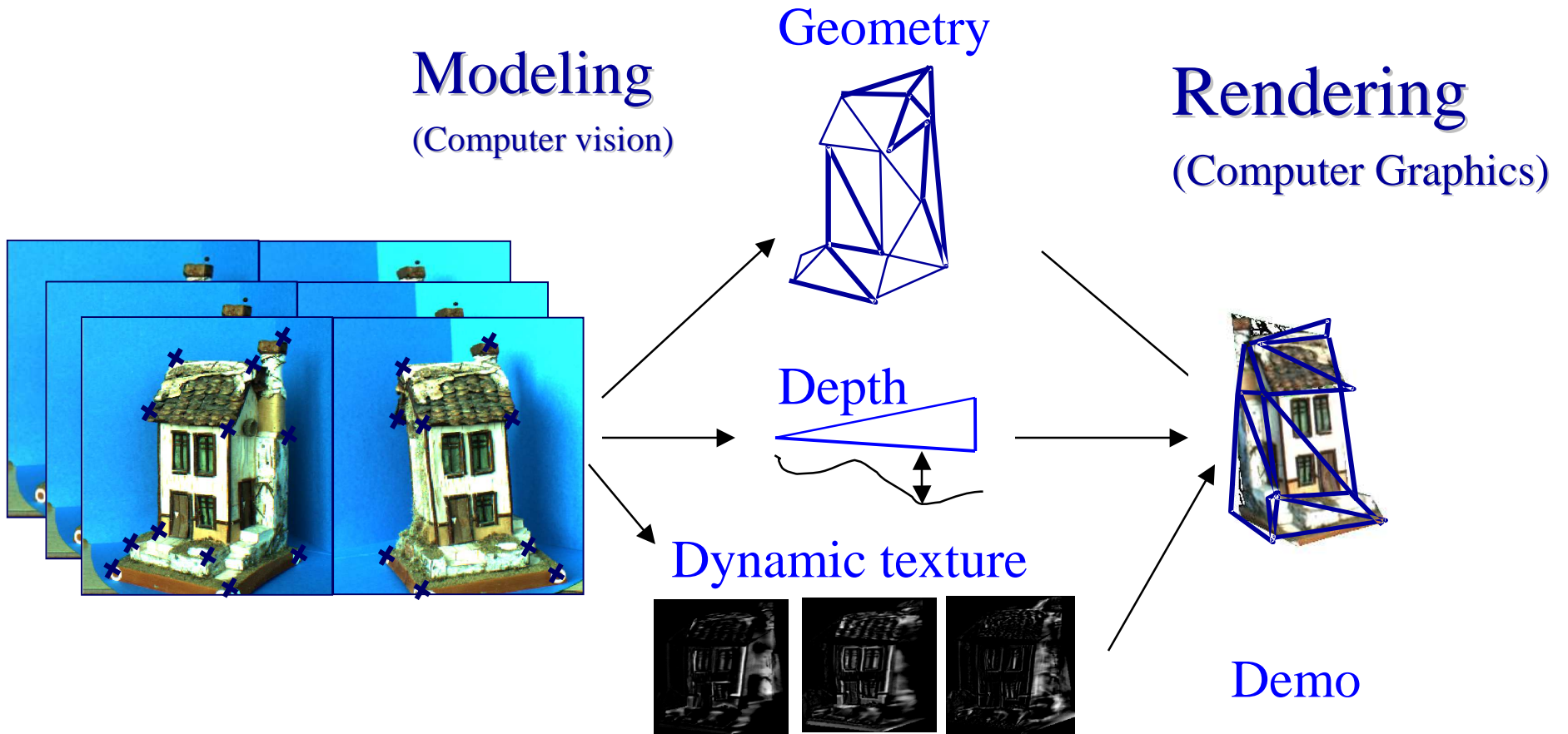


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Geometry alone does not solve modeling! Need: Multi-Scale Model



Multi-Scale model: **Macro** geometry, **Meso** depth, **Micro** texture

Three scales map naturally to CPU and GPU hardware layers

Key issue: Efficient memory access and processing

1. Macro: Conventional geometry processing

2. Meso: Pixel shader

- Fixed code, variable data access

3. Micro: Shader or Register comb.

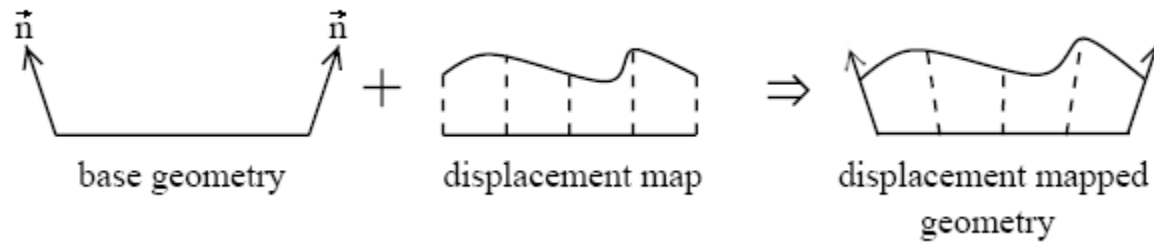
- Fixed code, fixed data access

Speedup

10x

10x

2. Meso Structure: Depth with respect to a plane



Flat texture



Displacement
mapped



Computing Meso structure: Variational shape and reflectance

Per-point cost function

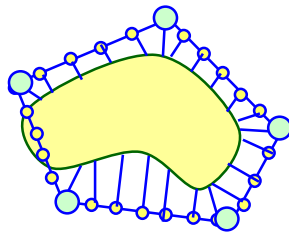
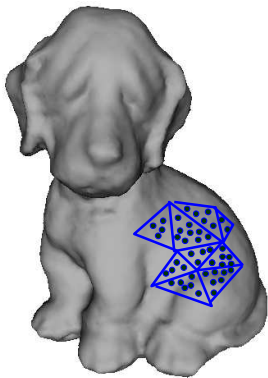
$$\Phi(\mathbf{X}, \mathbf{n}) = \sum_i h(\mathbf{X}, P_i) \|I_i(P_i(\mathbf{X})) - R(\mathbf{X}, \mathbf{n}, \mathbf{L}_i)\|$$

↑
Visibility+sampling

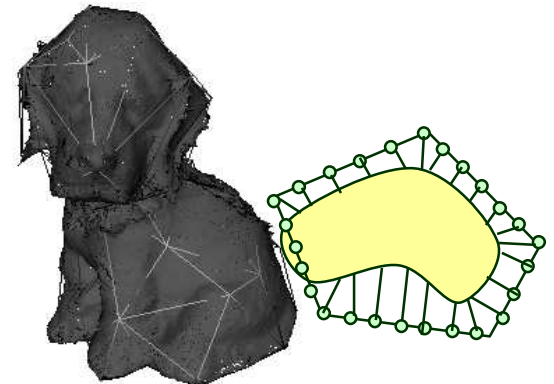
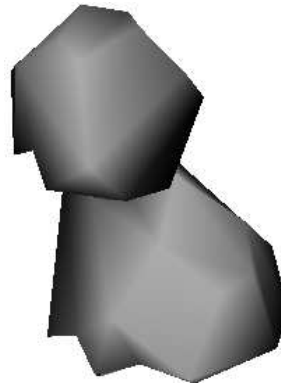
↑
reflectance

$$\frac{\partial S}{\partial t} = (2\Phi k - \langle \nabla \Phi, \mathbf{n} \rangle) \mathbf{n}$$

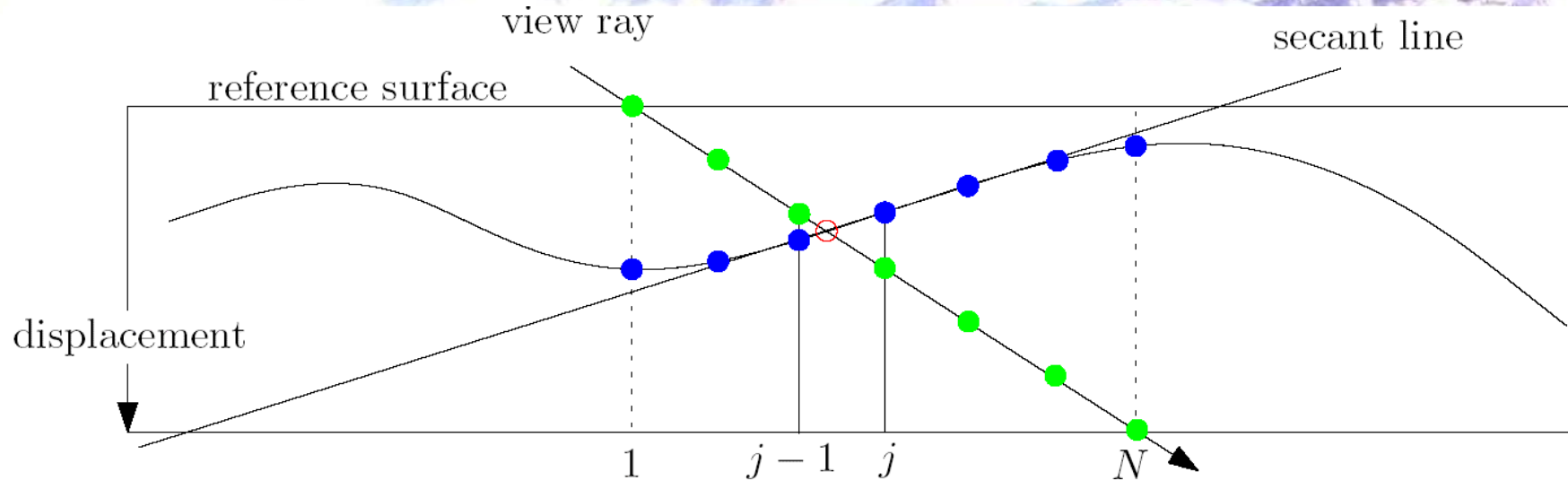
Deformable mesh



Depth from Base



Rendering Meso Structure: GPU: 83 pixel shader instructions



1. Sample d and ray at N (say 15) points.
2. Find point location j of intersection
3. Approximate d with line, calculate intersection
4. Potentially iterate if needed for accuracy

Results:

Over 100 fps on consumer graphics cards



3. Micro structure: Spatial texture basis

Modulated texture



Traditional texture



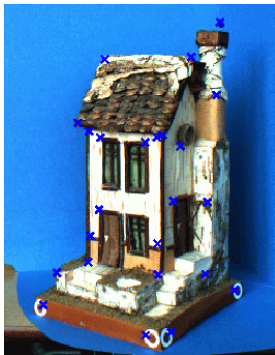
⇒ fixed execution and data access pattern

⇒ very fast implementation in graphics hardware

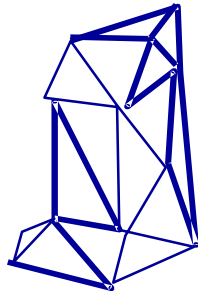
How/why do dynamic textures work?

3D geometry and texture warp map between views and texture images

View



Re-projected
geometry



Texture

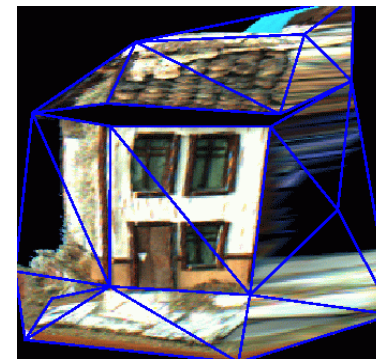
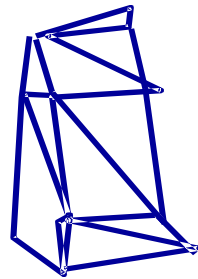


Texture
warp



Problem:

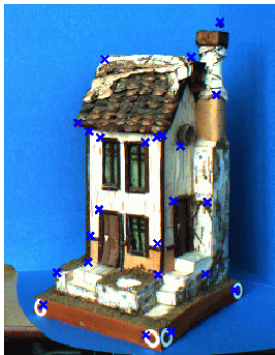
**Texture
images
different**



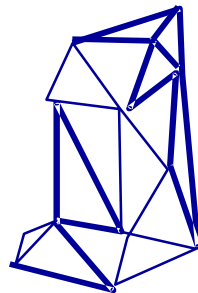
Sources of errors:

3D geometry and texture warp map between views and texture images

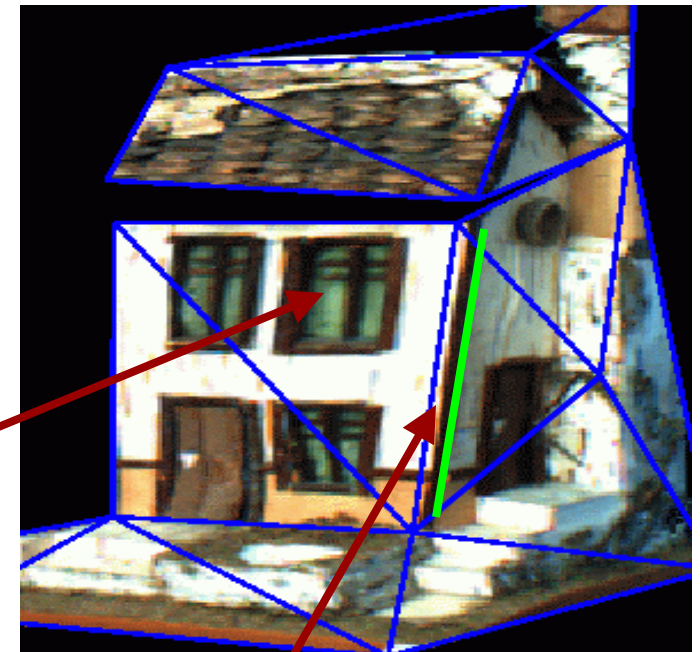
View



Re-projected
geometry



Texture



Texture
warp

**2: Out of plane error:
Object surface \neq texture plane**

1: Planar error: Incorrect texture coordinates

Spatial basis intro

1. Moving sine wave can be modeled:

$$\begin{aligned} I(t) &= \sin(u + at) \\ &= \sin(u) \cos(at) + \cos(u) \sin(at) \\ &= \sin(u)y_1(t) + \cos(u)y_2(t) \end{aligned}$$

Spatially fixed basis

2. Small image motion

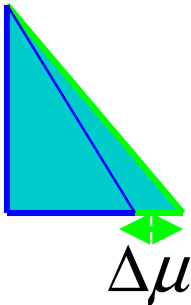
$$I = I_0 + \frac{\partial I}{\partial u} \Delta u + \frac{\partial I}{\partial v} \Delta v$$

Spatially fixed basis

Linear basis for spatio-temporal variation

On the object/texture plane:

- Variation resulting from small warp perturbations
- Taylor expansion:


$$= \text{triangle} + \frac{\partial}{\partial \mu} (\text{triangle}) \Delta \mu + h.o.t.$$

Small if $\Delta \mu$ small
and T_0 smooth

$$T(\text{view}) = T_0 + \frac{\partial}{\partial \mu} T_0 \Delta \mu + h.o.t.$$



Similarly: Can derive linear basis for out of plane and light variation!

Geometric spatio-temporal variability

Martin Jagersand
U of Alberta

Image “warp”

$$T(\mathbf{x}) = I(W(\mathbf{x}, \mu))$$

Image variability caused by an imperfect warp

$$\Delta T = I(W(\mathbf{x}, \mu + \Delta\mu)) - T_w$$

First order approximation

$$\Delta T = I(W(\mathbf{x}, \mu)) + \nabla T \frac{\partial W}{\partial \mu} - T_w = \nabla T \frac{\partial W}{\partial \mu}$$

Concrete examples

- Image plane
- Out of plane

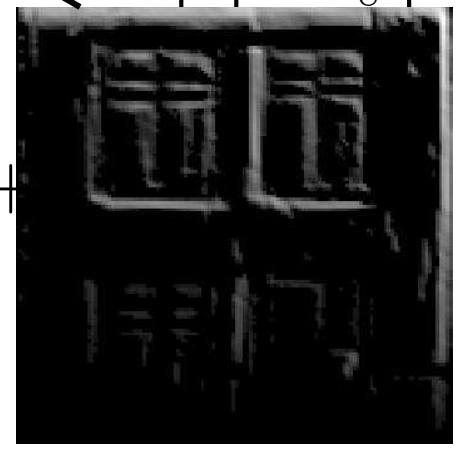
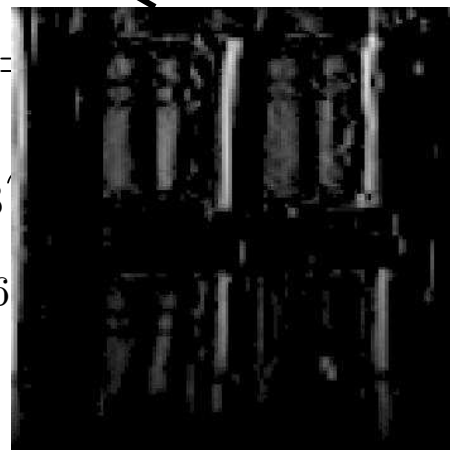
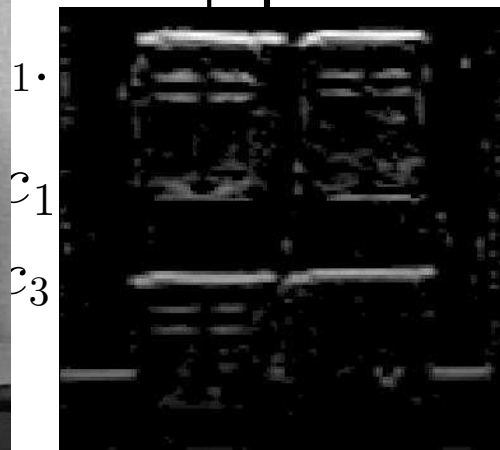
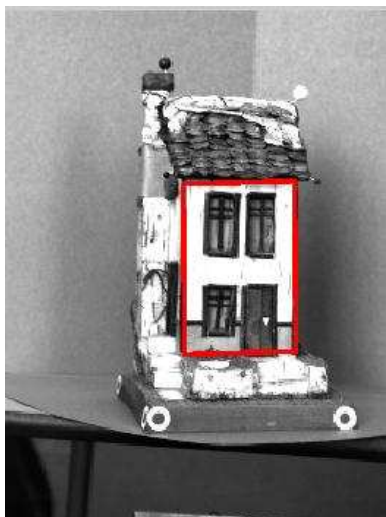
Variability due to a planar projective warp (homography)

- Homography warp

$$\begin{bmatrix} u' \\ v' \end{bmatrix} = \mathcal{W}_h(\mathbf{x}_h, \mathbf{h}) = \frac{1}{1+h_7u+h_8v} \begin{bmatrix} h_1u & h_3v & h_5 \\ h_2u & h_4v & h_6 \end{bmatrix}$$

- Projective variability:

$$\Delta \mathbf{T}_h = \frac{1}{c_1} \begin{bmatrix} \frac{\partial \mathbf{T}}{\partial u} & \frac{\partial \mathbf{T}}{\partial v} \end{bmatrix} \begin{bmatrix} u & 0 & v & 0 & 1 & 0 & -\frac{uc_2}{c_1} & -\frac{vc_2}{c_1} \\ 0 & u & 0 & v & 0 & 1 & -\frac{uc_3}{c_1} & -\frac{vc_3}{c_1} \end{bmatrix} \begin{bmatrix} \Delta h_1 \\ \vdots \\ \Delta h_8 \end{bmatrix}$$



Out-of-plane variability

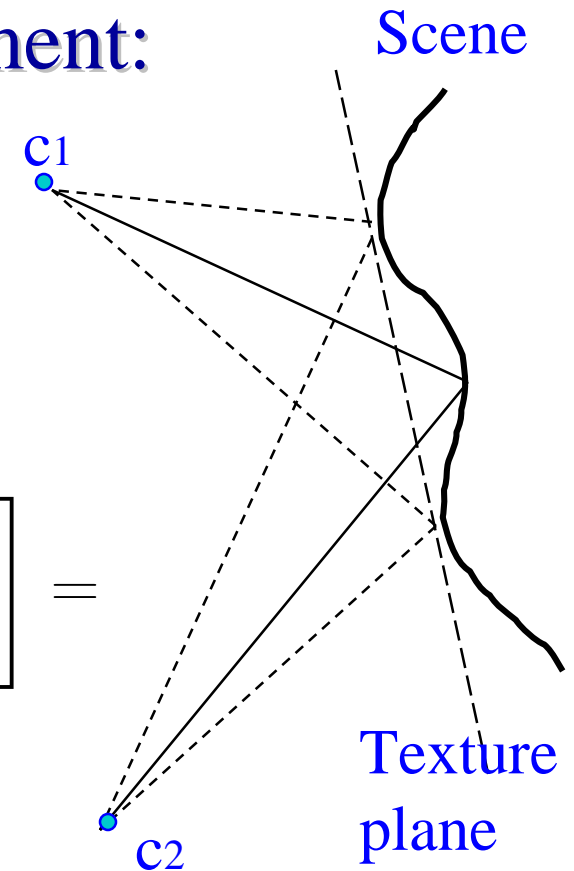
- Let $r = [\alpha, \beta]$ angle for ray to scene point
- Pre-warp texture plane rearrangement:

$$\begin{bmatrix} \delta u \\ \delta v \end{bmatrix} = \mathcal{W}_p(\mathbf{x}, \mathbf{d}) = \mathbf{d}(\mathbf{u}, \mathbf{v}) \begin{bmatrix} \tan \alpha \\ \tan \beta \end{bmatrix}$$

Depth w.r.t. model facet

- Texture basis

$$\begin{aligned} \Delta \mathbf{T}_p &= \mathbf{d}(\mathbf{u}, \mathbf{v}) \begin{bmatrix} \frac{\partial \mathbf{T}}{\partial \mathbf{u}} & \frac{\partial \mathbf{T}}{\partial \mathbf{v}} \end{bmatrix} \begin{bmatrix} \frac{1}{\cos^2 \alpha} & \mathbf{0} \\ \mathbf{0} & \frac{1}{\cos^2 \beta} \end{bmatrix} \begin{bmatrix} \Delta \alpha \\ \Delta \beta \end{bmatrix} = \\ &= \mathbf{B}_p \mathbf{y}_p \end{aligned}$$



Photometric variation

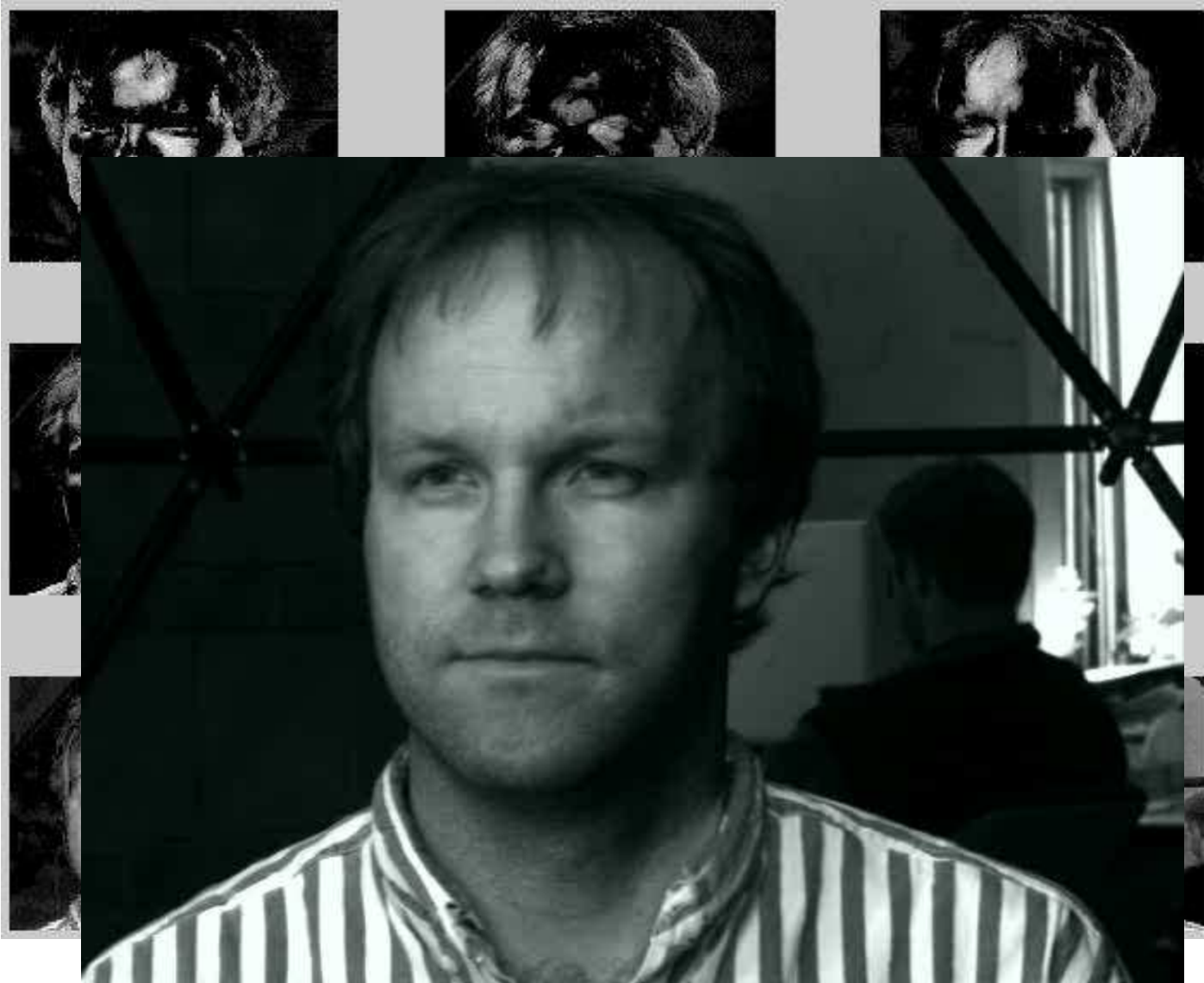
Analytic formula for irradiance for a convex Lambertian object under distant illumination (with attached shadows)
- spherical harmonics

[Barsi and Jacobs, Ramamoorthi and Hanrahan 2001]

$$T(\alpha, \beta, \theta, \phi) \approx \sum_{l=0}^2 \sum_{k=-l}^l L_{lk}(\alpha, \beta) A_l Y_{lk}(\theta, \phi)$$

$$T = [B_1 \cdots B_9][L_1 \cdots L_9]^T$$

Example of photometric variation



Composite variability

Similarly, composite texture intensity variability

$$\Delta \mathbf{T} = \Delta \mathbf{T}_s + \Delta \mathbf{T}_d + \Delta \mathbf{T}_l + \Delta \mathbf{T}_e$$

Planar Depth Light Res Err

Can be modeled as sum of basis

$$\begin{aligned} \Delta \mathbf{T} &= \mathbf{B}_s \mathbf{y}_s + \mathbf{B}_d \mathbf{y}_d + \mathbf{B}_l \mathbf{y}_l + \Delta \mathbf{T}_e \\ &= \mathbf{B} \mathbf{y} + \Delta \mathbf{T}_e \end{aligned}$$

How to compute?

From a 3D graphics model:

1. Texture intensity derivatives
 2. Jacobian of warp or displacement function
- Results in about 20 components:
 - T_0
 - 8 for planar,
 - 2 out-of plane (parallax),
 - 3-9 light

From video:

- We can expect an approximately 20dim variation in the space of all input texture images.
=> Extract this subspace

How to compute from images (cont)...

1. Take input video sequence, use SFS/SFM geometry to warp into texture space

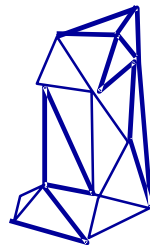
Input Images



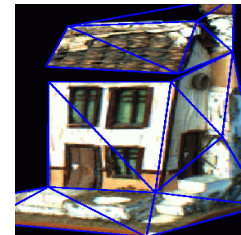
...



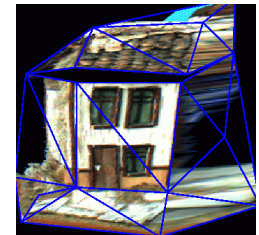
Geometry



Texture
warp



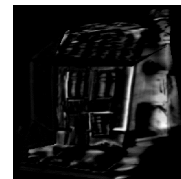
...



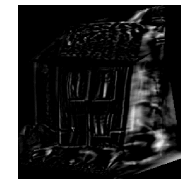
PCA

2. Extract a 20-dim
subspace through PCA

TexDemo



...



Are analytic image derivatives and PCA basis the same?

- Same up to a linear transform!

- Experimental verification: planar homog



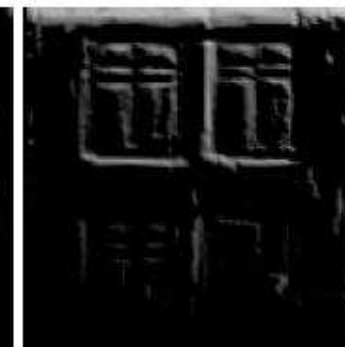
(a)



(c1) 1



(d1) 4



(e1) 7



Derivatives



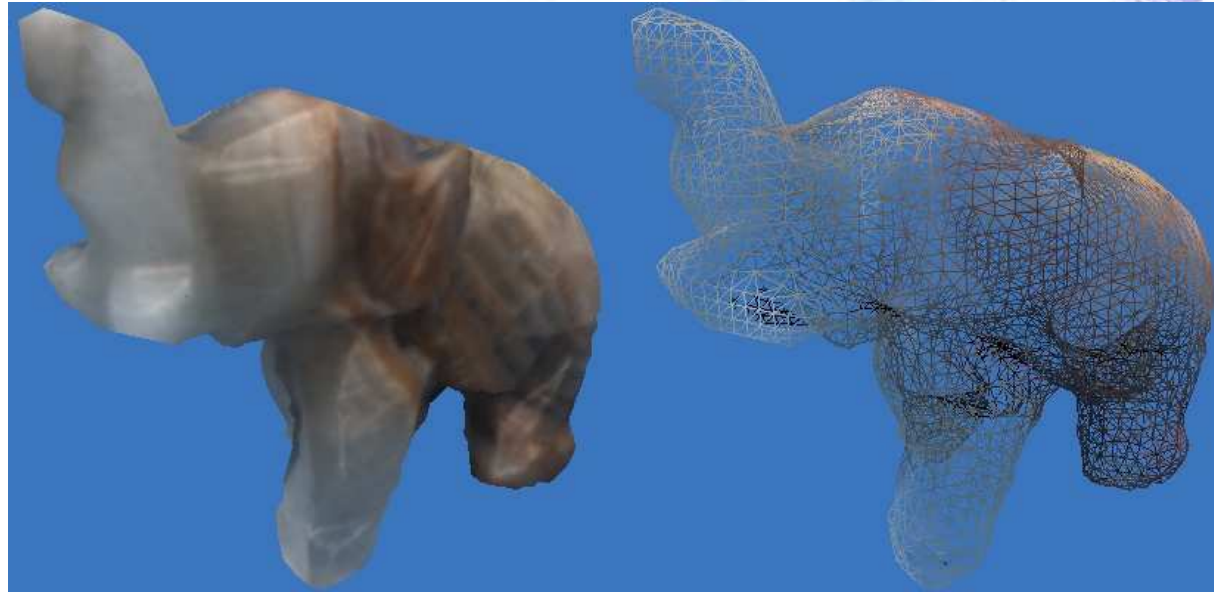
99%

agreement



PCA

Example renderings from 3D models



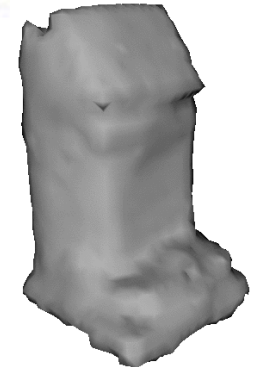
Recap: hierarchical model scale levels

Martin Jagersand
U of Alberta

1. Macro:

- SFM, SFS can generate coarse geometry but not detailed enough for realistic rendering
- Integrate tracking and structure computation

Scale: dozen pixels and up



2. Meso :

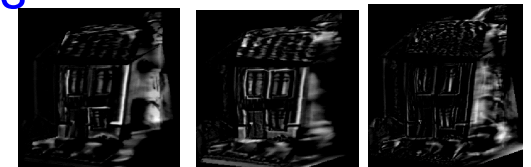
- Refine coarse geometry and acquire reflectance– variational surface evolution

Scale: 1-dozen pixels



3. Micro spatial basis :

- Represents appearance and corrects for small geometric texture errors limited by linearity of image Scale: 0-5 pixels



Comparison

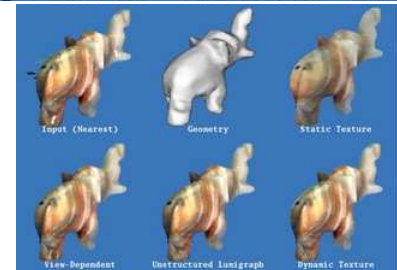
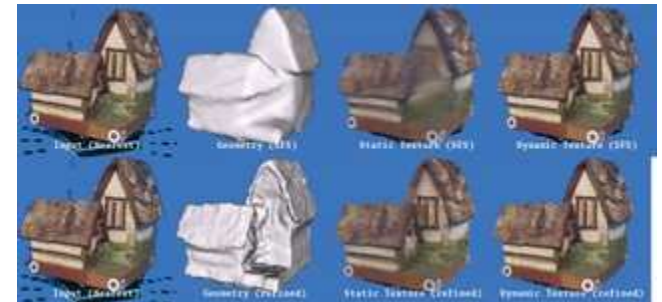
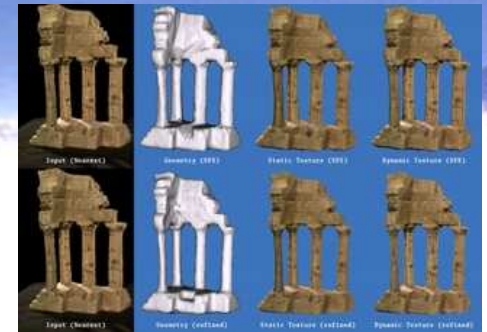
1. **Static texturing:** (Many, e.g. Baumgartner et al. 3DSOM)
 - Average color projected to point.
 - Better: Pick color minimizing reprojection error over all input imagesWorks when model geometry is close to ground truth and light simple
2. **Viewdependent texture** (Debevec et al)
 - Pick color from closest input photograph (or interpolate from nearest 3)Works when possible to store large numbers of images
3. **Lumigraph / Surface light field** (Buehler et al / Wood et al)
 - Store all ray colors (plenoptic function) intersecting a proxy surfaceWorks if proxy surface close to true geometry
4. **Dynamic texture** (Ours: Jagersand '97/ Matusik / Ikeuchi99 / Vasilescu04...)
 - Derive a Taylor expansion and represent derivatives of view dependencyWorks for light and small (1-5 pixel) geometric displacements.

videos

From Simple to Complex Scenes

4 test cases

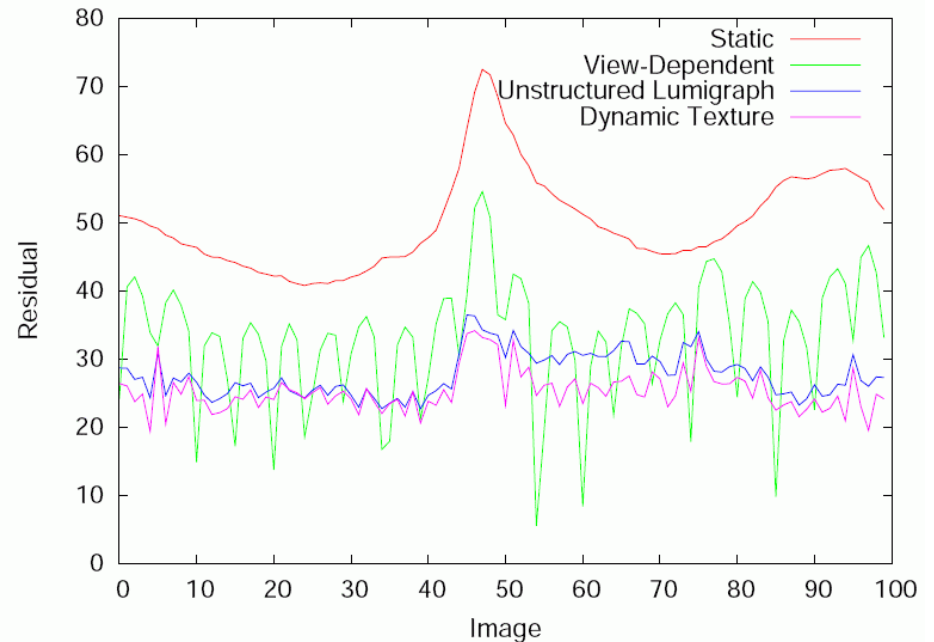
1. Simple Geom: SFS alone ok
2. General Geom: SFS + Variational Shape and Reflectance fitting (+View dep texture)
3. Complex Light: Dynamic Texture / Lumigraph
4. Challenge for Computer Vision



From Simple to Complex Scenes

4 test cases

1. Simple Geom: SFS alone ok
2. General Geom: SFS + Variational Shape and Reflectance fitting (+View dep texture)
3. Complex Light: Dynamic Texture / Lumigraph
4. Challenge for Computer Vision



Vision

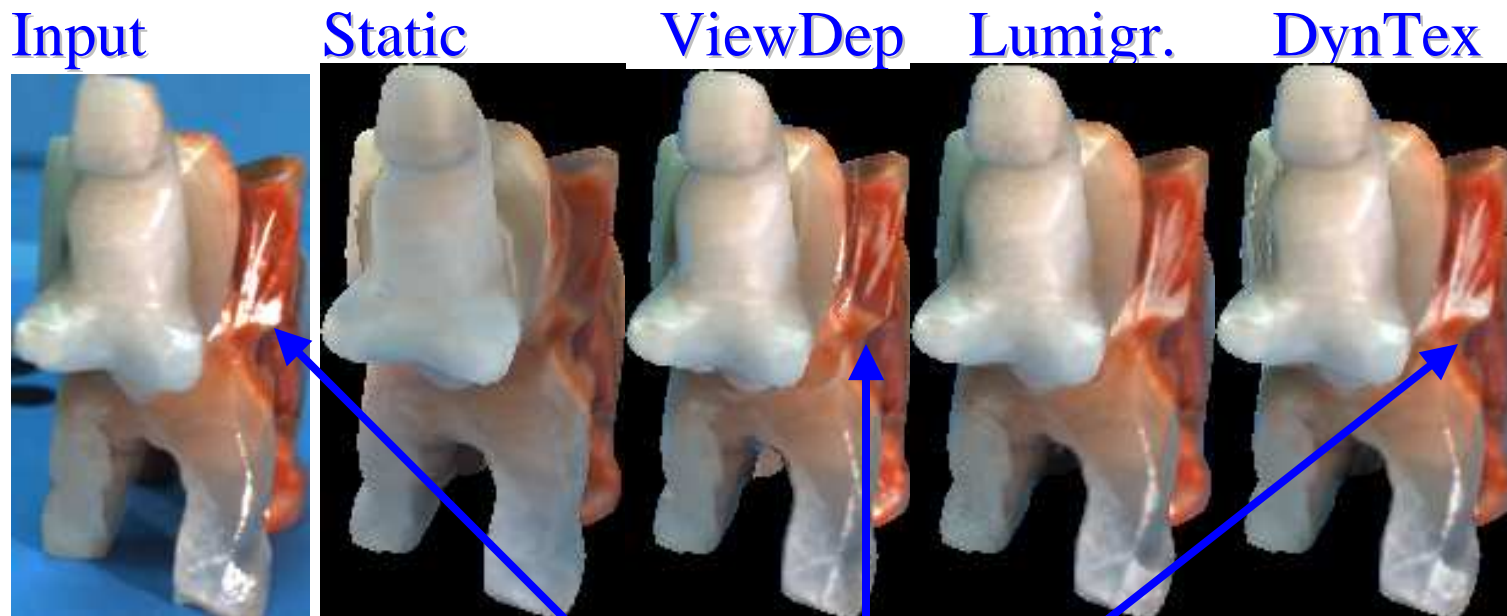
err (var)	temple	house	eleph.	wreath
Static	10.8(1.5)	11.8(1.2)	19.0(1.4)	28.4(2.8)
VDTM	8.3(1.9)	9.8(1.3)	10.1(1.9)	21.4(3.5)
Lumigr	10.8(2.5)	9.8(1.2)	5.9(0.7)	14.3(1.3)
DynTex	7.3(1.0)	9.4(1.0)	6.6(0.7)	13.4(1.2)

Table 1. Numerical texture errors and variance. %-scale.

Example of render differences

- Jade Elephant

- Complex Reflectance (specularities and scattering)



Specular highlight

Tracking with a dyntex model + AR

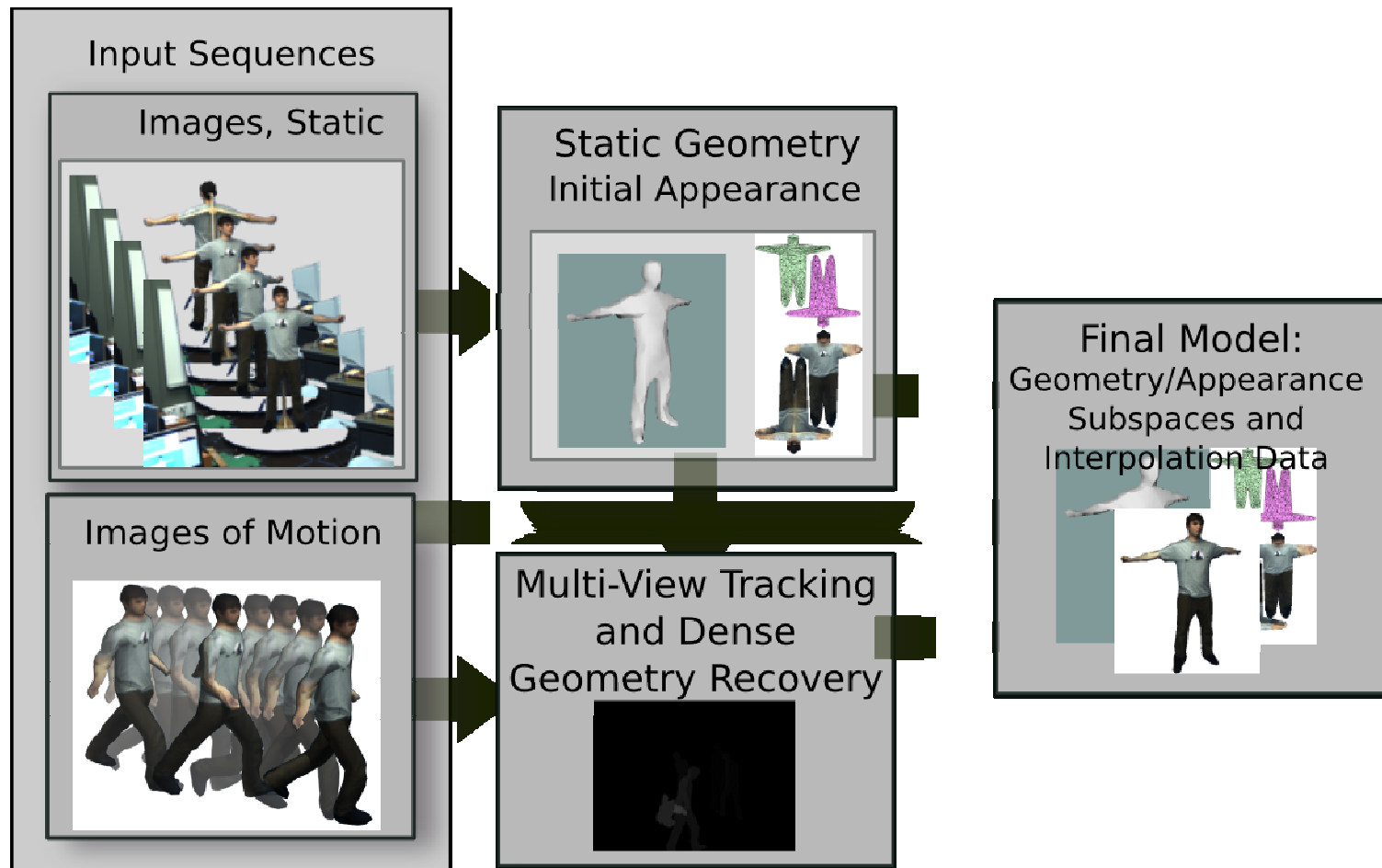
Successful: 0/5
Border Lost: 2 Orient Lost: 0
Thresh 128



Mode=Pattern
All Corners: off (Sub-Pixel: off)
FPS: 1.000000

Capturing non-rigid animatable models

current PhD project, Neil Birkbeck



Capturing non-rigid animatable models



For better movies see:
<http://webdocs.cs.ualberta.ca/~birkbeck/phd/>

Questions?

More information:

- Downloadable renderer+models

www.cs.ualberta.ca/~vis/ibmr

- Capturing software + IEEE VR tutorial text

www.cs.ualberta.ca/~vis/VR2003tut

- Main references for this talk:

Jagersand et al “Three Tier Model” 3DPVT 2008

Jagersand “Image-based Animation...” CVPR 1997

- More papers: www.cs.ualberta.ca/~jag

Questions?

CAMERA-BASED 3D CAPTURE SYSTEM

- Dow

- Cap

- Mai

- More papers: www.cs.ualberta.ca/~jag